

# Caballero, Simsek: A risk-centric model of demand recessions and macroprudential policy

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January 2018

## Model summary

- time-variation in risk/volatility
- zero lower bound
- contribution of speculation under heterogeneous beliefs

## Empirical/quantitative questions and challenges

- Fluctuations in risk-free rate and risk premia
  - role of intertemporal elasticity of substitution
- Extent of speculation
  - magnitude of fluctuations in the wealth distribution

## Capital accumulation

$$\frac{dk_{t,s}}{k_{t,s}} = g_{t,s}dt + \sigma_s dZ_t$$

- volatility regimes  $s \in \{1, 2\}$ ,  $\sigma_1 < \sigma_2$  ( $s = 1$  is the 'good' state)
- endogenous investment choice (Q-theory) determines  $g_{t,s}$

## Output

$$y_{t,s} = A\eta_{t,s}k_{t,s}$$

- capital efficiency  $\eta_{t,s} \leq 1$ , efficient level  $\eta_{t,s} = 1$ .

## Endogenous price of capital $Q_{t,s}$ (locally predetermined)

$$\frac{dQ_{t,s}}{Q_{t,s}} = \mu_{t,s}^Q dt$$

Aggregate resource constraint  $c_{t,s} + i_{t,s} = y_{t,s}$

Logarithmic preferences, belief  $\lambda_s$  about leaving state  $s$  (jump intensity)

- Constant wealth-consumption ratio

$$c_{t,s} = \rho Q_{t,s} k_{t,s}$$

- Heterogeneous beliefs as an extension (later)

Optimality condition for the portfolio choice

- Merton-type optimal choice of risky investment ( $\omega_{t,s} = 1$  in eqm)

$$\omega_{t,s} = \frac{1}{\sigma_s^2} \left( \underbrace{\frac{\overbrace{A\eta_{t,s} - \iota_{t,s}}^{\text{net rental rate}}}{Q_{t,s}} + \overbrace{g_{t,s} + \mu_{t,s}^Q}^{\text{capital gain}}}_{\text{return on capital } r_{t,s}^k \text{ conditional on } s} + \lambda_s \underbrace{\frac{M_{t,s'} Q_{t,s'} - Q_{t,s}}{M_{t,s} Q_{t,s}}}_{\text{return on capital cond. on jump}} - r_{t,s}^f \right)$$

## Characterization

- previously defined objects are functions of  $s$  only
- economy homogeneous degree 1 in capital (conditional on  $s$ )

## Efficient equilibrium: in each state

- efficient output produced ( $\eta_s = 1$ )
- easy to verify that  $Q_s = Q^*$ , consistent with  $c_s = c^* k_s$ , and  $i_s = i^* k_s$
- hence  $r_s^k = r^k$
- Merton's optimality condition implies

$$r_s^f = r^k - \sigma_s^2$$

- this establishes correct risk premium while supporting capital price  $Q^*$

## Logarithmic preferences

- price of capital constant, risk-free rate adjusts to clear asset markets

## ZERO LOWER BOUND

Now consider the **zero-lower bound restriction**

$$r_s^f \geq 0.$$

- when  $\sigma_s^2$  high, asset markets cannot clear (violation of  $r_s^f = r_s^k - \sigma_s^2$ )

In order to generate correct risk premium,  $r_s^k$  has to rise, hence  $Q_s$  must fall

$$r_s^k = \frac{A\eta_s - \iota_s}{Q_s} + g_s + \lambda_s \frac{M_{s'}}{M_s} \frac{Q_{s'} - Q_s}{Q_s}$$

- $Q_s < Q^*$  associated with a lower level of **current** economic activity
  - due to  $c_s = \rho Q_s k_s$ , when  $Q_s$  falls, consumption  $c_s$  must fall too  $\implies \eta_s < 1$
- $Q_s < Q^*$  associated with a lower level of **future** economic activity
  - lower investment rate  $\iota_s$  reduces capital growth rate  $g_s$
- demand-driven recession
- belief about recovery  $\lambda_s$  an additional factor

## Asset market equilibrium condition

$$r_s^f = \left( \underbrace{\frac{A\eta_s - \iota_s}{Q_s} + g_s}_{\text{return on capital } r_{t,s}^k \text{ conditional on } s} + \lambda_s \underbrace{\frac{M_{s'} Q_{s'} - Q_s}{M_s Q_s}}_{\text{return on capital cond. on jump}} \right) - \sigma_s^2$$

When is the zero-lower bound problem more severe?

1. volatility  $\sigma_s^2$  is high
2. growth rate of economy  $g_s$  low (e.g., inefficient investment)
3. agents believe transition into good states ( $Q_{s'} > Q_s$ ) is less likely ( $\lambda_s$  low)
4. agents believe transition into bad states ( $Q_{s'} < Q_s$ ) is likely ( $\lambda_s$  high)

Agents differ in **subjective probabilities of regime transitions  $\lambda_s$**

- pessimists believe recessions more likely, recoveries less likely
- optimists vice versa

What now matters is the **wealth-weighted average belief** about transition.

Agents engage in speculative trades

1. in the **good state, optimists sell insurance** on jumps into the bad state
  - lose wealth when transition occurs
  - this wealth loss reduces the wealth-weighted belief about recovery
  - exacerbates the recession and further constrains output
2. In the **bad state, optimists bet on recovery**
  - when recovery does not happen, optimists keep losing wealth
  - further exacerbates the recession

Speculative positions determine wealth dynamics

- agents do not take into account the **zero lower bound externality**
- larger speculative positions imply larger wealth loss of the optimists in the recession state

**Simple macroprudential policies**

- limiting the extent of speculation can improve welfare
- careful considerations of alternative definitions of welfare

## Carefully written paper

- very clean modeling choices
- excellent discussion of the underlying mechanisms

## Emphasizes externality from the zero lower bound

- similar to the literature with financial constraints
  - Bernanke, Gilchrist and Gertler; Brunnermeier and Sannikov; He and Krishnamurthy, etc.
- **financial constraint externality**: valuations must support an additional constraint in the intermediary sector
  - requires inefficient balance sheet adjustment

## Does the story hold quantitatively?

- requires proper calibration of two important channels

Authors deliver sharp results using **logarithmic preferences**

- constant wealth-consumption ratio
- absent ZLB, fluctuations in the value of capital must be absorbed by fluctuations in risk-free rate

$$\sigma_s^2 = r_s^k - r_s^f$$

**Other extreme**  $IES = \infty$

- constant risk-free rate, all adjustment through the price of capital

Substantial disagreement about the value of  $IES$

- micro vs. asset pricing
- here the key is to nail the asset price dynamics
- use estimated values from **asset pricing studies**:  $IES \approx 1.5 - 2$

Fluctuations in risk/volatility then **partly absorbed by efficient fluctuations in the price of capital**

- asset market clearing condition

$$\sigma_s^2 = r_s^k - r_s^f$$

- fluctuations in  $r_s^k$  mitigate fluctuations in  $r_s^f$
- alleviates the zero lower bound problem

Introducing belief heterogeneity adds degrees of freedom

- direct calibration to shifts in the wealth distribution desirable

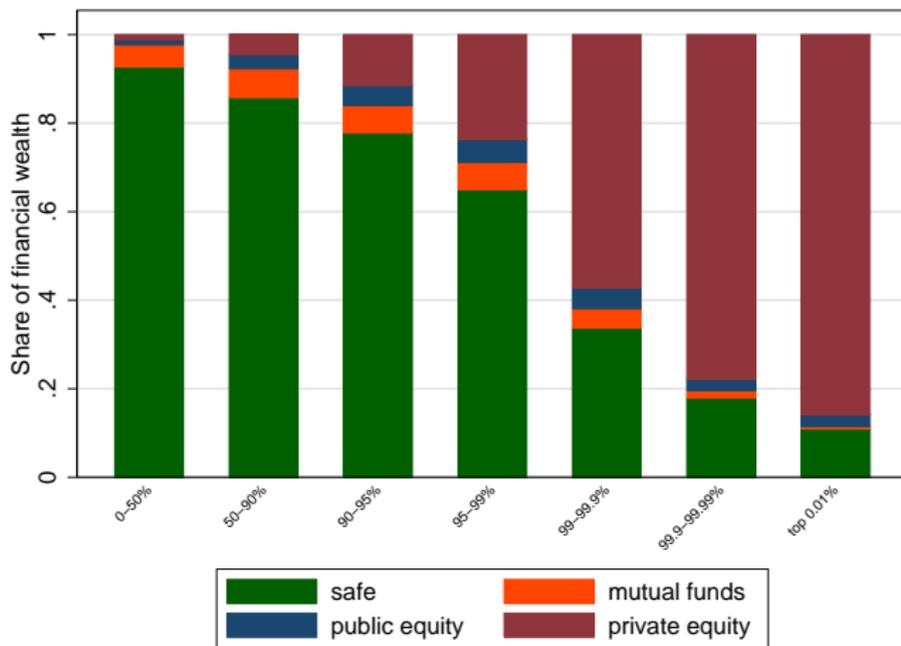
What **wealth distribution**? Depends on interpretation.

- households
- financial institutions

Fluctuations in the **wealth distribution of households**

- e.g., Fagereng, Guiso, Malacrino, Pistaferri (2016)
- substantial idiosyncratic risk in returns (underdiversification)
- limited systematic short-horizon churning
  - strong systematic effects over longer horizons

## Portfolio allocation across the wealth distribution



## Heterogeneity in returns over time

